



# Intricacies of System of Systems Operational Availability and Logistics Modeling

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# Overview

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- Background and definition of operational availability ( $A_o$ ) and system of systems (SoS)
- SoS  $A_o$  equations
- SoS  $A_o$  complexities
- Example SoS  $A_o$  simulation results

# System $A_o$

- Operational Availability ( $A_o$ ) is the portion of time that a system is either operating or capable of operating
- $A_o$  is calculated, estimated, and modeled for
  - A specifically defined collection of **hardware**
  - Performing specifically defined **operations**
  - Over a specifically defined **timeframe**
  - With specifically defined **reliability** and **maintainability** operational performance characteristics, and
  - Specifically defined **sustainment** assumptions
- Any reported  $A_o$  reflects and depends upon all the above assumptions
- Comparison of  $A_o$  to requirements, other system  $A_o$ , or across tradeoffs requires “synching up” above definitions to make comparisons valid

**Definitions and assumptions must be addressed for each intended use of  $A_o$  models**

# A<sub>o</sub> Definitions

- Well-understood, high-level A<sub>o</sub> definition

$$\begin{aligned}A_o &= \frac{Uptime}{Uptime + Downtime} \\ &= \frac{Total\ Time - Downtime}{Total\ Time} \\ &= \frac{Operating\ Time + Operable\ Time}{Operating\ Time + Operable\ Time + Downtime}\end{aligned}$$

- Operable time (or standby time) usually defined as part of A<sub>o</sub>

- Common equation estimator of A<sub>o</sub>

$$A_o = \frac{MTBF}{MTBF + MDT}$$

where MTBF is Mean time Between Failures and MDT is Mean Down Time

- Results in static, steady-state estimation of A<sub>o</sub> if steady state MTBF and MDT are used
  - Not valid for short durations that do not reach steady state
- MTBF can be scaled by utilization for intermittent use systems



# System of Systems

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- SoS definition
  - A SoS is comprised of a set of systems, each performing a defined task or mission, in which at least one system can be dependent on one or more other systems
    - SoS level performance is emerging and cannot be assessed by assessing individual system performances separately, except for the case where the systems operate (and are maintained) independently of each other
    - System dependencies can be of varying complexity and include:
      - Required sequential or parallel system tasks
      - System functional redundancies
      - K of N systems operating
      - Combinations of these
- SoS are more prevalent than ever
  - More autonomous systems functioning with other systems
  - Increased network-centric functionality
  - Effectiveness and requirements established for increased system synergies accomplishing increasingly complex missions

# SoS $A_o$ Equations

- Case 1: If all systems in the SoS operate and are maintained independently, the SoS  $A_o$  is equal to the product of the individual system  $A_o$ s

$$SoS A_o = \prod_{i=1}^n A_{oi} \quad \text{where } A_{oi} \text{ is the } i^{th} \text{ independent system } A_o$$

- Case 2: If all systems are dependent, such that if any one system fails the remaining systems stop operating, the SoS  $A_o$  can be solved as a function of the individual system  $A_o$ s

$$SoS A_o = \frac{1}{1 - n + \sum_{i=1}^n \frac{1}{A_{oi}}} \quad \text{where } A_{oi} \text{ is the } i^{th} \text{ independent system } A_o$$

**Rarely does a SoS operate as Case 1 or Case 2**



# SoS $A_0$ Calculations

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- SoS  $A_0$  equation calculations have limited application
- Complicating factors that negate the use of estimating equations for SoS  $A_0$ 
  - Systems within the SoS not all in series
  - Systems not all independent or not all dependent
  - Systems not all operating all of the time
  - Complicated logistics strategies
  - Sustainment limitations, including spares, maintainers, special equipment
  - Short duration of operations, making the steady-state result not relevant
- Simulation modeling is usually required to capture complex operating, operable, and down time hours of a SoS
- System of Systems Analysis Toolset (SoSAT) simulation used to analyze and provide SoS  $A_0$  for an example problem

# SoSAT Background and Applications

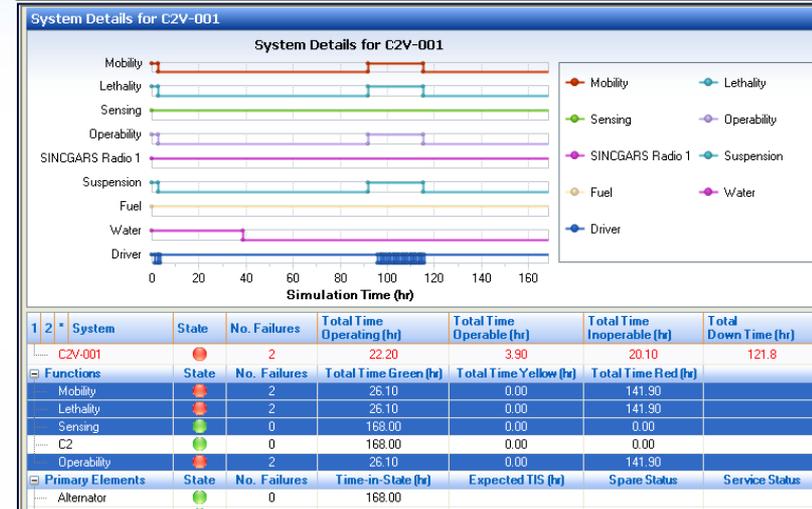
- SoSAT (System of Systems Analysis Toolset) is a suite of software tools:
  - State modeling tool
  - Stochastic simulation tool
  - Advanced data visualization tools
  - Reliability, consumables, and supply chain optimization tools
- Initially designed to provide DoD and military services capability to analyze large systems of systems and their various platforms across multiple mission scenarios to assess multiple key performance parameters
  - Supported multiple US Army Future Combat Systems (FCS) trade studies
  - Supported US Army PEO Integration with modeling and analysis of Logistics, Sustainment, Reliability Key Performance Parameters for Capability Packages
  - US Army PEO Ground Combat Systems (PEO GCS) using SoSAT for Fleet Management and Modernization Planning initiative
  - JPO MRAP using SoSAT for MATV assessments and analyses
  - Participating in formal Verification, Validation & Accreditation effort with Army Organizations (AMSAA and ATEC)
  - Navy Littoral Combat Ship Mission Modules using SoSAT for modeling and analysis

- **SoSAT v1.0 released October 2007**
- **SoSAT v1.5 released October 2008**
- **SoSAT v2.0 released January 2010**
  - **SoSAT v2.0 simulation verified and validated (V&V'd) by the US Army**
  - **Availability calculations and algorithms officially accredited by the US Army**
- **SoSAT v3.0 in development**

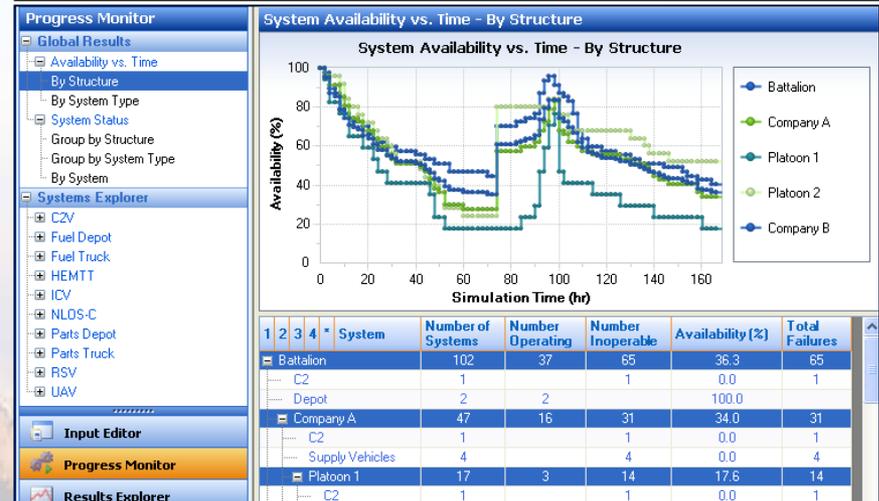
# SoSAT Capabilities

- SoSAT provides analysts the capability to
  - Simulate *any or all* of a system of systems (SoS) organizational structure
  - Simulate multiple mission segments for a SoS
  - Provide data to assess SoS performance objectives
  - Support business decisions and trade-offs
- Basic Modeling Features
  - System element reliability failures
  - Consumable usage and depletion
  - Maintenance activities including any required spares or services
  - Supply reorder for consumables and spare inventories
- Advanced Modeling Features
  - Damage effects modeling
  - Network modeling
  - Prognostics and Health Management
  - Time-based changes to model attributes
  - System Referencing (interdependencies)
  - Human performance
- Active Model Development
  - Advanced network modeling
  - Enterprise modeling

## Tracks individual system components and functional availability over time



## Track SoS functional availability and statistics over time



# SoSAT Platform Modeling Concepts

- Platform as a System State Model

- Multiple user defined functions/operations
- Multiple States (not just functional or failed)
- Models interdependencies
- Can include external factors (weather, terrain, combat, etc.) that affect the overall system or just the system elements

- Model system behavior by defining:

- States for all subsystems/components/functions
- How transitions are made between states

- States can change through:

- Normal processes (failure, repair, etc.)
- External conditions (weather, terrain, combat, etc.)
- Changes in functional states of other systems

## Platform as a System State Model



System Model

### Example Elements

- 105 mm Cannon
- M240 Machine Gun
- Sandstorm

### Example Operations

- Operability
- Lethality
- Mobility

**The System State Model is an intuitive way to capture system behavior and is the building block for systems in the simulation**



# Mission Profile Complexities

- ***Is the mission profile executed as planned even if System A experiences failures?***
  - Depending on the scenario being modeled, failures of system A could cause a shift of the profile and extend the mission beyond 7 days
  - In this example scenario, the scheduled operating periods are missed and the schedule would proceed as planned
- ***What systems are required to be up for the SoS to be up?***
  - This reliability block diagram is accurate for representing the SoS reliability, from a reliability perspective, at time of failure
    - If any system fails, the SoS fails



- However, this RBD does not apply for  $A_0$  over the entire mission
- ***Systems required to be up can vary over the mission profile for a SoS***

# Mission Profile Complexities (cont.)

- *What happens if System A fails on Day 3 and is down for 24 hours?*

Day>	1	2	3	4	5	6	7
System A	■ ■	■ ■ ■	■				
System B			■	■ ■ ■	■ ■	■ ■	■
System C	■ ■	■ ■ ■	■ ■	■ ■ ■	■ ■	■ ■	■
System D	■ ■ ■ ■ ■ ■ ■						

- The affect on  $A_0$  depends on specifics of the scenario being modeled
- The SoS represented could be a ship transiting through an area that requires System A in one region and System B in another
  - In this case, the series RBD is not valid for  $A_0$  because the RBD is dynamic



# System A<sub>0</sub> Complexities

- *A<sub>0</sub> can be reported for the individual systems operating as part of the SoS, but for what time period?*
  - A<sub>0</sub> can be reported for:
    - The entire 7 day mission period
    - The portion of the mission that system has an active role
    - The specific segments when the system was scheduled to be operating
  - In many cases, all three periods are of interest, requiring additional statistics to be gathered during a test or simulation
- *If System C fails, does System A go to an operable state?*
  - The actual SoS this example was based on was a helicopter (System C) with payloads (Systems A and B)
  - If System A failed, System C would not operate
  - Similarly, if System C fails, System A would not operate
  - SoS assessment must account for these periods of dependency that result in additional operable time for non-failed systems



# Dependency Effects on System $A_o$

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- $A_o$  measures the availability in the operational environment
  - Up time includes operating time and operable time
- When a system operates outside the context of a SoS, operable time is a function of system utilization
  - A system that is scheduled to run for 18 hours/day has a utilization of 0.75
- Within a SoS, there can be additional operable time due to system dependencies
  - Direct dependencies, such as System A not being used because System C is down
  - Indirect dependencies, such as unrelated systems occasionally causing the SoS to move to an area for repairs, limiting the operating time of other systems

# Dependency Effects on System $A_o$ (cont.)

- System dependencies can cause unexpected results
  - An improvement to one system's reliability can cause lower performance measures of other systems
    - A system experiences operable time if it is waiting for another system it depends on to be repaired
      - Operable time is counted as up time in the  $A_o$  calculation for the dependent system
    - A system could operate more if another system it depends on is improved
      - Reliability and maintainability improvements could cause all systems within the SoS to operate more
  - Time that was previously categorized as operable time will be replaced by additional operating time and down time

**$A_o$  for a dependent system can decrease after an improvement to a system it depends on**

# Mean Down Time Complexities

- MDT, in isolation, can be a misleading statistic
- A reliability improvement to a system within a SoS can cause an increase in the SoS MDT
  - Suppose a SoS meets the SoS MDT requirement but does not meet the SoS MTBF requirement
  - A reliability improvement is made to a system that fails frequently
  - SoS MTBF now meets the requirement, but SoS MDT has increased and no longer meets the requirement
  - This unexpected result can occur if the repair times of the improved system are less than the SoS MDT
    - The total downtime is less as a result of the reliability improvement
- The effect of MTBF changes on MDT can be seen within an individual system, but SoS assessment is necessary to see the SoS MDT impact

**MDT is most useful when combined with MTBF  
in an  $A_0$  calculation**



# Logistics

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- Logistics delays are an important part of MDT
  - Large delays can be incurred when waiting on parts, consumables, and personnel if correct planning has not taken place
- Critical to plan for spares, consumables, and personnel for systems operating within a SoS
  - Spare parts quantities, consumables, and personnel requirements for a system may differ when the system is considered operating in a SoS versus independent of the SoS
    - For example, within the SoS, a system may not operate as much as it would on an independent mission requiring less resources
    - If multiple systems within the SoS require the same repair skill type, additional delays can occur if the resource is limited and already in use

**Space, weight, and personnel constraints can be traded off amongst individual systems to maximize SoS metrics**

# SoS $A_0$ Simulation Calculation

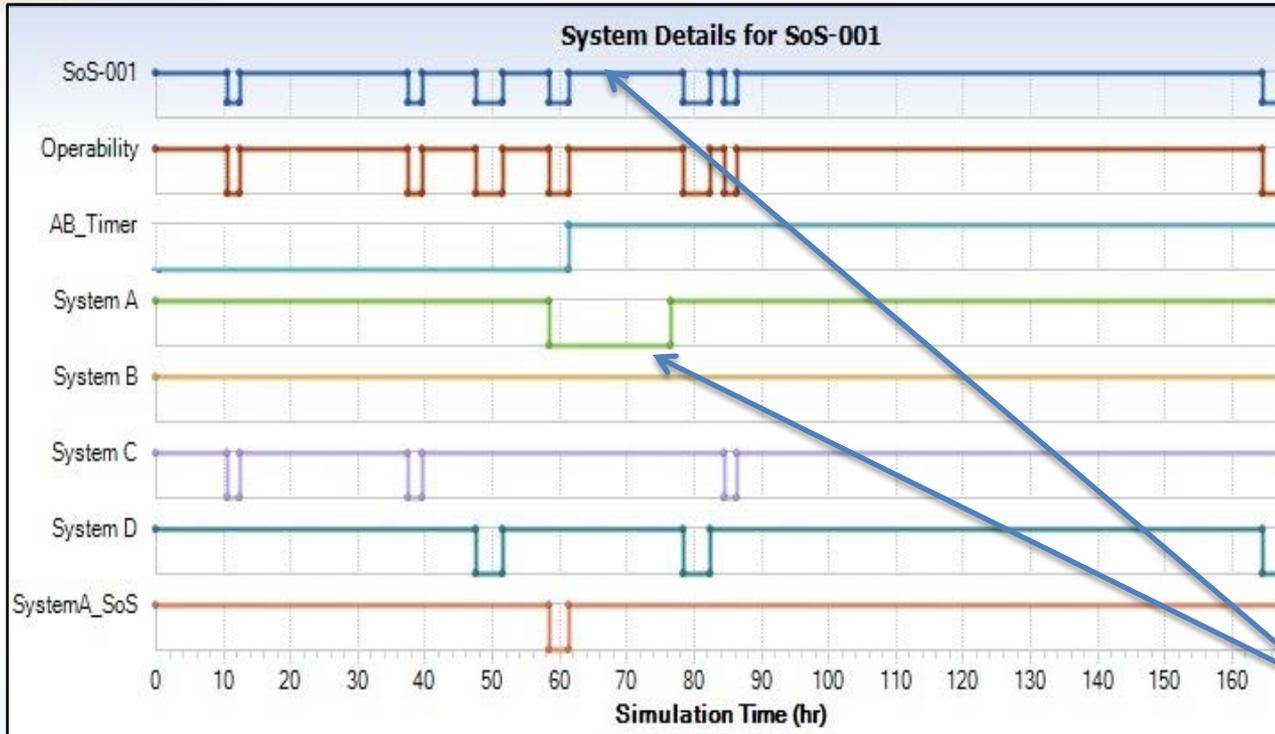
- SoS  $A_0$  is calculated by this equation through simulation

$$A_0 = \frac{Uptime}{Uptime + Downtime}$$

- Simulation allows for complex mission and system definitions and dependencies
- The sample SoS was simulated assuming the following attributes of Systems A - D

System	MTBF	MDT	Scheduled Operating Hours
A	20	18	10
B	50	12	18
C	25	2	28
D	500	4	168

# SoS $A_o$ Simulation Results



- The lines represent the status of systems, user defined functions, and the SoS
- When a line dips down, the item it represents is in a down state
- Not all System A downtime results in SoS downtime

System Details		System	Time Operating	Time Operable	Time Inoperable	Time Down	Availability	Total Failures
1	2 *	SoS	373.754	548.280	10.874	75.092	0.915	4.796
		SoS-001	156.098	0.000	0.000	11.902	0.929	1.850
		System A-001	9.273	153.219	4.955	0.553	0.967	0.306
		System B-001	17.022	146.593	3.567	0.818	0.974	0.368
		System C-001	24.148	141.968	0.852	1.032	0.989	0.942
		System D-001	166.713	0.000	0.000	1.287	0.992	0.330

SoS  $A_o$

# Scheduled vs Actual Operating Time

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- Each system operates less time than scheduled because of failures and dependencies
- This mission could be repeated many times by this system or a fleet of systems
- Fuel Usage and sparing estimates should be based on performance within the SoS.

# SoS Instantaneous Availability vs. Time



- $A_0$  for the SoS was 0.929 for the entire mission
- SoS performs much better once operations shift from System A to System B
  - System B has a higher MTBCF and a lower MDT than System A

**Instantaneous  $A_0$  can vary throughout the mission depending on the current activity**



# Summary

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- Systems of systems are becoming more prevalent than ever with increased use of autonomous systems and network-centric functionality
- System interdependencies and complex interrelated sustainment operations that exist in a SoS present complexities in calculating or estimating  $A_o$ 
  - In most cases, simulation modeling is required
- Analyzing SoSs with accurate accounting for interactions is complex, but is crucial to obtaining meaningful and accurate SoS results